Use of the 'Perceptron' algorithm to distinguish translational initiation sites in E. coli

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ABSTRACT

We have used a "Perceptron" algorithm to find a weighting function which distinguishes E. coli translational initiation sites from all other sites in a library of over 78,000 nucleotides of mRNA sequence. The "Perceptron" examined sequences as linear representations. The "Perceptron" is more successful at finding gene beginnings than our previous searches using "rules" (see previous paper). We note that the weighting function can find translational initiation sites within sequences that were not included in the training set.

INTRODUCTION

A translational initiation region, or ribosome binding site, may be defined by rules. In the previous paper we (1) showed that stronger rules can be built by including information from about 35 bases of mRNA surrounding the initiation codon. The number of such possible rules, even if one only varies bases at the positions of information peaks, is very large. Even then, if we absolutely require any specific feature, we will miss some known genes. For example, the Shine and Dalgarno region is considerably variable and one gene, the P_{RM} transcript for cI of lambda, has no nucleotides 5' to the AUG (2). Even the AUG is not absolutely required; our current library of genes contains four cases of GUG initiation codons (1), and two occurrences of UUG have been reported (3, 4). Furthermore, AUA can serve to initiate protein synthesis at low rates in vivo (5). Essentially any RNA polymer can be made to initiate translation under appropriate ionic conditions in vitro (6).

We imagine that the ribosome scans mRNA, and translational initiation may occur with some probability at any site. For regions without a proper initiation codon or Shine and Dalgarno, the probability is essentially zero. Having an AUG increases the probability and a nearby Shine and Dalgarno increases the probability further. Other nucleotides in the vicinity can influence the probability. "Favorable" nucleotides can compensate for a poor Shine and Dalgarno, and, perhaps, "unfavorable" nucleotides can negate a good

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Shine and Dalgarno. Secondary structure will influence the probability as well (7).

We will try here to define a probability function based solely on linear sequences. The goal will be to find a mathematical function W, for weighting function, such that applying W to any sequence will give a value, and the magnitude of that value will determine whether that particular sequence is a ribosome binding site. Stated more rigorously, we want to find a function W such that the product W.S is greater than some threshold, T, if and only if the sequence S is a ribosome binding site.

Researchers in the field of artificial intelligence have for years investigated methods of automated pattern recognition. In the late 1950's, a class of parallel feature detection systems with learning capabilities, called "perceptrons", was developed by Frank Rosenblatt (8). In their book Perceptrons, Minsky and Papert (9) prove the "Perceptron Convergence Theorem" which shows that if a solution exists (of the kind the perceptron is capable of reaching), that solution will be found in a finite number of steps (see also 10). Though the method has not been particularly successful for the kind of plane geometry problems initially contemplated, it seemed well suited for our attempt to find a separation function for linear nucleic acid sequences.

METHODS

Data Base

The data base is the mRNA Library described in the previous paper
(1). It contains 78,612 bases of transcribed RNA on which reside (at least)
124 genes. The potential genes of T7, noted by Dunn and Studier (11), are not included in this set, nor are they included in any of the nongene sets.

Encoding the Sequences

We have chosen to encode the sequences in a matrix of $4 \times N$ elements, where N is the length of the sequence. All elements are either 1 or 0; 1 represents the presence of a base at a position, and 0 represents the absence. Any column can have at most a single 1, so the matrix is quite sparse. The seven long sequence ACGGTAC is encoded as:

							7
A	1	0	0	0	0	1	0 1 0
С	0	1	0	0	0	0	1
G	0	0	1	1	0	0	0
T	0	0	0	0	1	0	0

We could, of course, have encoded the four bases into only two bits, but then some combinations of bases at any position would have been ambiguous. For instance, if we had used the encoding

we could not distinguish (by the algorithm to be described) between classes where the determining feature was an A or T versus a C or G. So as to not bias our work against such combinations we used the four bit encoding. (This also allows us to have sequences with no bases at some positions, as occurs when an mRNA begins close to the initiation codon.)

Perceptron Algorithm

The task is to find a weighting function, W, such that W·S > T if and only if S is a ribosome binding site. (By W·S we mean the multiplication of each element in S by the corresponding element in W, and then the sum of those products.) Such a W and T would serve to distinguish ribosome binding sites (sequences in S^+) from all other sites (sequences in S^-). The algorithm can be described by the following three step procedure (9):

test: choose a sequence S from S^+ or S^- if S is in S^+ and $W \cdot S \geq T$ go to test if S is in S^+ and $W \cdot S < T$ go to add if S is in S^- and $W \cdot S < T$ go to test if S is in S^- and $W \cdot S \geq T$ go to subtract

add: replace W by W + S

go to test

subtract: replace W by W - S

go to test

Figure 1 is an example of how this works in detail. The perceptron convergence theorem (9, 10) guarantees that, if a solution exists, the solution will be found in a finite number of steps. The number of steps may, however, be extremely large. We decide whether or not a solution will be found by examining the number of changes to W that take place during each round of learning, where a round of learning consists of examining each sequence. If the number of changes plateaus for many rounds we terminate the process and assume a solution doesn't exist (see Figure 3).

Data Flow and Programs Used

All programs used (Table 1) are written in Pascal and are part of the Delila system (12). Figure 2 shows the flow of data and the programs used.

Figure 1. We show an example of the perceptron algorithm applied to some nucleotide sequences. The sequences S $^+$ and S $^-$ represent different classes. The threshold is 0. W $_1$ is an arbitrary starting point. The "Perceptron Convergence Theorem" guarantees that a solution will be found (if one exists) regardless of the starting W.

The mRNA Library and the gene instructions set are made as described in the previous paper (1). The first nongene set used was those sequences found by rule 2 of that paper. New nongenes were found, using the program PatSer, from various sublibraries of the mRNA library, until no new sites were found in the

TABLE 1
List of Programs Used

Name	Version	Purpose
Concat	1.00	Concatenate text files
Delila	1.20	Librarian: extracts libraries
		based on Delila instructions
PatAn	1.10	Analyzes a W matrix
PatLrn	2.01	Based on "Perceptron" algorithm,
		generates a W matrix which
		distinguishes two sets of
		sequences
PatLst	1.10	Listing of a W matrix
PatSer	1.10	Searches a library with a W matrix
		and identifies all sites
		evaluated above some
		threshold; produces Delila
		instructions to get those
		sites
PatVal	1.10	Evaluates a library of sequences by
		a W matrix
Sepa	1.07	Separates Delila instruction sets

entire mRNA library.

RESULTS AND DISCUSSION

Random Sequences

In the example of the perceptron algorithm (Figure 1), it is clear that many other solutions exist, depending on the choice of W₁. Separating two S⁺ sequences from two different S⁻ sequences when the sequences are five long is, in fact, trivial. At what number of sequences, of a given length, does the ability to find a separating W become significant? An equivalent problem is determining the probability of finding a hyper-plane that will separate two sets of points in N dimensions. That remains an open question, but clearly increasing the number of points (different sequences) in either set decreases

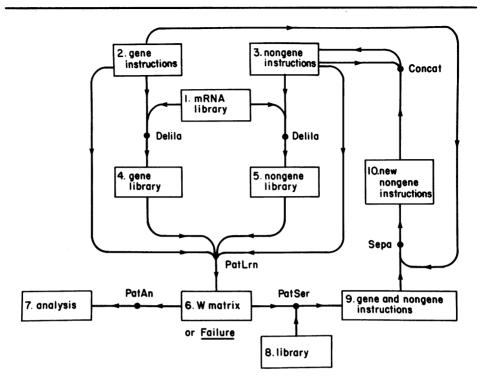


Figure 2. Flow diagram. Boxes represent data files (described in the text) and dots represent programs (described in Table 1). The arrows indicate the direction of information flow. If PatLrn does not find a solution in a user-specified number of rounds, that failure is noted and the program is terminated. When the searched library (Box 8) is the entire mRNA library (Box 1) and no new nongenes are found (that is, Box 10 is empty), that W matrix (Box 6) serves to distinguish the gene beginnings from all other sites.

the probability of separation, as does decreasing the number of dimensions (shortening the sequences). We tested for significance using 75 arbitrarily chosen 101-long sequences (from MS2 and G4) to represent the S⁺ class. We then tried to find a W which would separate them from a library of less than 20,000 coliphage bases. The answer is that such a W does not exist (Figure 3). Therefore, if we can separate 124 sites (of 101 nucleotides) from a library of over 78,000 bases that result is highly significant. If we can succeed with shorter sequences the answer becomes more significant. Gene Beginnings

i) 101-long sequences

The gene set was all 124 known starts in the mRNA library. The first set of nongenes was the 167 sites found by rule 2 of the previous paper (1).

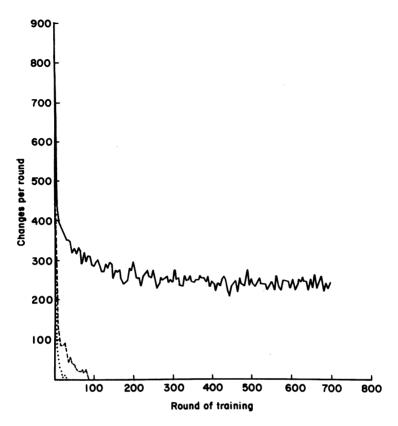


Figure 3. We show the number of changes to the W matrix per round of training for different data sets. A round of training is the examination of each sequence in the larger class (S⁺ or S⁻) exactly once. Sequences in the smaller class will be examined at least once. The three experiments are: 75 arbitrarily chosen phage sequences versus 1074 other phage sequences, each 101 bases long (———); the 124 genes versus 1034 nongenes, each 101 bases long (…..); the 124 genes versus 1082 nongenes, each 71 bases long (———).

W was initialized as all zeros. The program PatLrn changed W until it separated the input sets. This W was used to search a sublibrary, MS2, (using the program PatSer) to find new sites which are wrongly classified as genes. Those sites were added to the nongene set and PatLrn used to find a new W that separates the genes from the nongenes. After nine cycles of using PatLrn and PatSer (on the mRNA library and various sublibraries, see Figure 2) a W was found which finds only the 124 known genes from the entire mRNA library. That matrix, W101, is shown in Figure 4. One would expect that the positions most important for the separation of S⁺ from S⁻ would show the largest

differences within the values in that column of W. A program which calculates the variance of the values in any column was written (PatAn) and the plot of those values is shown in Figure 5. As expected, the initiation codon has the greatest variance and the Shine and Dalgarno region is next. Otherwise, peaks of values occur over approximately the same region as was shown previously to contain information (1).

ii) 71-long sequences

Since we expect that the ribosome interacts with at most 35 or 40 bases of mRNA, we want to find a W of about that size to distinguish genes from other sites. We next narrowed the region we used to -40 to +30 from the initiation codon. After six more rounds of adding new nongenes, a solution was found. That matrix, W71, is shown in Figure 6, and its variance curve is shown in Figure 7.

iii) 51-long sequences

The process was continued by looking only at the nucleotides from -30 to +20. This time PatLrn failed to find a separating W. Since the variance curve of Figure 7 shows little information 5' of -20, but does show some 3' of +20, we also tried to find a W to separate on the region of -20 to +30. This also failed. While one might be tempted to infer that the ribosome uses information from more than the 51 nucleotides we have examined, we believe that inference to be incorrect. In our mRNA library, there must be hidden translational initiation sites unknown to us, and therefore included in the nongene set of sequences. Even a single such sequence of typical initiation strength might prevent separation of the two sets. In the successful longer sequence separations, the perceptron takes into account additional bases which may, in fact, be irrelevant to the ribosome. Furthermore, we have intentionally taken into account only the primary sequence and have not considered the role of secondary structure. This flaw could prevent further reduction of the size of the matrix to 35 or 40 bases even when we are confident of the genes and nongenes. If we could accurately predict what the secondary structure of the mRNAs were, we could include that in the learning process and perhaps find a W which succeeds on short sequence windows.

In the absence of such a secondary structure predictor we have continued with the learning process. The program (PatLrn) allows the user to specify different thresholds for genes and nongenes. That is, one can require that W.S \geq T for S a ribosome binding site, and W.S < T' for all other sites. By making T' > T one can search for a W which doesn't completely separate the genes from all other sites but rather allows for some overlap between the two

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POSITION: -60 -59 -58 -57 -56 -55 -54 -53 -52 -51 -50 -49 -48 -47 -44 -45 -44 -43 -42 -41 -40 -39 -38 -37 -36 -35
    A : 7 -2 13 -2 -8 -13 -18 5 0 -5 13 8 -15 9 -4 -7 9
                                                            0 -8 -11 -10 -6 -7 -5 -6 -12
    6 -5 2
    6 : -6 -9 -7 0 8 -16 -4 -2 -16 1 -4 8 -14 5 11 -13 -24 3 7 22 -11 -9 -15 10 -4
    T: 5 1 -3 9-14 7 15 -5 3-16-17 4 18 5 -3 -1 2 4 5 -5 7 8 -5-15 6 3
POSITION: -34 -33 -32 -31 -30 -29 -28 -27 -26 -25 -24 -23 -22 -21 -20 -19 -18 -17 -16 -15 -14 -13 -12 -11 -10
    A : -1 -27 -3 -6 0 -12 -3 -4 -7 14 -2 -4 -6
                                                0 12 5 -9 0 -11 -11 10 8
    C: -14 -3 -8 -10 -21 2 0 -2 -1 -11 -3 -1 5 -11 -4 7 0 -14 6 -8 -20 -7 -36 -44 -15
   -6: -5 -6 -3 -1 -4 -1 -4 -15 0 -14 3 10 -19 -3 -10 -7 -7 7 1 -8 -6 15 21 42 35
    T : 4 16 -4 7 11 -4 -1 12 8 10 -1 1 8 2 -10 -16 11 1 -3 16 -3 -36 -8 -27 -53
POSITION: -9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
    A : -3 -5 4 -20 -11 5 6 -2 -15 66 -69 -52 -5 -4 6 8 -24 -7 -10 -7 13 14 -9 -18 14
     C : -50 -43 -35 -38 -29 -29 1 -9 1 -87 -55 -64 -45 11 -22 -14 -20 -15 -15 -10 -22 -5 2 6 6
    6 : 22 16 -6 -5 -15 -25 -33 -28 -53 -36 -50 107 -5 -37 -44 -27 -15 -23 -16 -29 -47 -17 -29 -15 -23
     T : -27 -26 -23 2 -7 -14 -40 -28 0 -53 75 -62 -20 -40 -10 -35 -5 -12 -1 4 14 -23 7 -2 -26
POSITION: 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
     A : -12 -42  1 -5 -4 -32  12 -10  20 -6 -1  3 -4  4 -10 -1 -2 -14  11  14 -3  2 -13
    C: -8 19 -7 9 -3 17 -2 3 -9 5 22 22 8 -1 1 18 6 11 -10 -8 7 10 0
                                                                              7 14 :
     6 : -7 -1 -6 -17 -4 0 -15 -14 -4 -17 -10 -5 -13 -8 10 -13 -13 9 -4 -3 10 2 4 -8 -21 :
     T: 1 4 -7 3 -4 0 -10 8 -18 7 -22 -21 8 4 -3 -6 7 -8 1 -5 -16 -16 7 -6 0 :
```

Figure 4. <u>W101</u>. All genes give values of at least 2 by this matrix. All other sequences in the mRNA library give values of 1 or less.

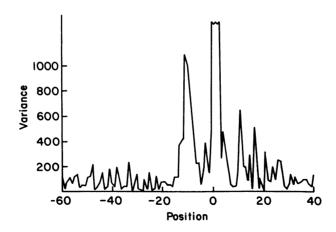


Figure 5. Variance of W101.

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POSITION: -40 -39 -38 -37 -36 -35 -34 -33 -32 -31 -30 -29 -28 -27 -26 -25 -24 -23 -22 -21 -20 -19 -18 -17
     A : -19 -16 -21 -8 1 2 -12 -45 -16 -9 9 0 -7 -7
                                                        9 30
                                                               5 -1 -16 -12 10
                                                                               3 -3 -11
     C : 2 2 3 -7 -14 -1 -17 -1 -21 -8 -20 -13 1 -2
                                                        4 -2
                                                               8
                                                                  3
                                                                    8 -9
                                                                              -2 14 5
     6 : -31 -18 -11 12 -14 -5 -7 -9 -12 -14 -14 0 -9 -4
                                                        5 -18 16 29 -8 -1 -5 -1
                                                                                   0 12
     T : 21 4 1-25 -4 -2 9 -1 -6 12 6 -9 -4 -1 16 24
                                                               2 21
                                                                     4 11 -12 -15 11 -10
POSITION: -16-15-14-13-12-11-10-9-8-7-6-5-4-3-2-1 0 1 2 3 4
     A : -9 -1 26
                   7 4 21 -8 -4 -14 -2 -17 -10 1 25 -6 -18 91-103 -74 -33 -16 -2 -1 -34
     C : -1 -21 -21 -9 -38 -63 -31 -60 -43 -37 -53 -39 -31 3 -18 -9-129 -91-114 -58 -9 -42 -19 -24
     6 : -10 -5 -16 22 32 59 50 31 36 4 -1 -24 -34 -55 -29 -65 -53 -86 142 -17 -38 -64 -60 -34
     T : 16 22 -5 -37 -16 -35 -73 -42 -54 -40 -5 -6 -16 -53 -27 12-105 87 -83 -25 -66 -19 -47 -32
POSITION: 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30
     A : -25 -29 -18 0 16 -3 -18 22 -14 -42 3 0 1 -23 20 -11 21
                                                                 4 -13 -15 -7
     C : -30 -21 -14 -29 7 14 16 2 -19 26 -18 16 -13 11 -9 2 -5 14 41 33
                                                                           1
     6 : -28 -12 -41 -52 -19 -37 -24 -36 -3 -7 4 -10 -8 -6 -12 -18 4 -21 -7 3 -18
     T : -23 6 17 25 -46 0 0 -15 11 14 9 1 7 5 -12 16 -30 -7 -31 -27 22
```

Figure 6. W71. All genes give values of at least 3 by this matrix. All other sequences in the mRNA library give values of 2 or less.

sets. The program doesn't, however, have a means of finding a "best" W of this type, either by minimizing the range of overlap or the number of nongenes in the overlap region. Rather, one must try different cases of T and T' until one is satisfied with the result.

Figure 8 is the matrix, W51, for which all genes give a value greater than 0 (T) and all nongenes give a value less than 30 (T'). The variance is

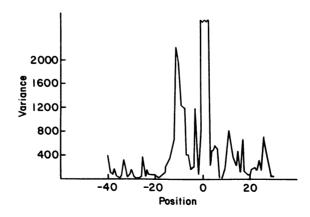


Figure 7. Variance of W71.

Figure 8. W51. All genes give values of at least 0 by this matrix. All other sequences in the mRNA library give values of 30 or less.

shown in Figure 9 and is quite similar to the gene χ^2 curve in the previous paper (1), except for a peak at position 17. While not totally separating all genes from all other sites, W51 does considerably better than any of the rules discussed in the previous paper, even the extended rule. This matrix finds all of the 124 genes, as being evaluated at greater than 0, and finds only 64 other sites with values as great. This is out of over 78,000 other sites. Figure 10 shows the range of values for genes and nongenes using this matrix. The nongenes shown represent the tail of a distribution of all the other sites, whose average value is about -900. One can generalize for W51 that sites with values greater than 30 are genes, sites with values less than

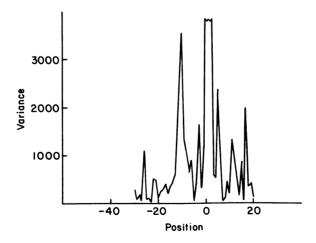


Figure 9. Variance of W51.

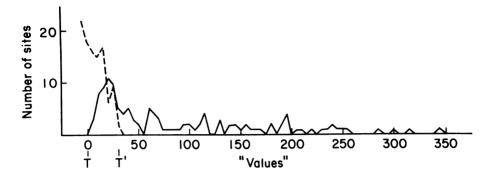


Figure 10. We show the values of genes (----) and nongenes (...) for W51. All genes give values of at least 0 (T) and all nongenes give values of 30 or less (T'). Most of the sequences in the mRNA library (over 78,000 bases) give values less than -5 and are not plotted.

O are not genes, and sites with values in between are of both classes. Predictive Value

In order to decide if the resulting Ws have learned distinguishing features of gene beginnings, as opposed to memorizing the training set, we tested them on new sequences which became available to us after our last library update. Table 2 compares the predictive ability of each of the three Ws and rule 2 of the previous paper. Surprisingly, W101 is by far the best predictor of gene beginnings. Not only does it find the most genes but it also finds the fewest other sites. Perhaps this means that the context of the ribosome binding site is important beyond the region of direct interaction with the ribosome as measured in an initiation complex (22). W51 and W71 both find fewer of the genes than rule 2 but also find fewer other sites; the ratio of genes found to nongenes found is higher using W51 or W71 than using rule 2.

The collection of genes in Table 2 is somewhat atypical for <u>E. coll</u> in that 3 of the 10 do not start with ATG; <u>tufA</u> begins with GTG while <u>rps20</u> and <u>ndh</u> start with TTG. Rule 2 (which requires an ATG) cannot identify these sites. If Rule 2 were changed to allow GTG and TTG, <u>tufA</u>, <u>rps20</u>, and <u>ndh</u> would be found, along with approximately 3 times as many nongenes as before. The W matrices, however, don't require an ATG, though that codon is favored at the initiation site. They all, in fact, properly classify the four GTG starts in the set of genes they were trained on. W101 finds the GTG start for <u>tufA</u>, and even properly identifies the TTG start of <u>rps20</u>, though there were no TTG starts included in the training set.

We have already used this method to identify the location of one gene.

	genes found/	nongenes found	1	
genes (ref)	rule 2 ¹	W101	W71	W51
rspB,tsf (13)	2/2	2/1	1/2	1/2
<u>lexA</u> (14, 15) ²	1/0	0/0	0/0	0/0
rpoD (16)	0/3	0/1	0/0	0/1
T4E, IPIII (17)	2/1	2/1	2/2	2/2
tufB (18)3	1/2	1/0	1/0	1/0
tufA (19)	0/2	1/0	0/0	0/0
rps20 (3)	0/0	1/0	0/0	0/0
ndh (4)	0/2	0/2	0/2	0/2
total 10 genes	6/12	7/5	4/6	4/7

TABLE 2
Predictive Ability of W Matrices

We received a preprint describing a 750 base-pair sequence including the T4 e (lysozyme) gene (17). Beyond the end of the e gene (position 583 in the sequence) is an ATG which is found by rule 2 and by each of our W matrices. That ATG is followed by an open reading frame through the end of the sequence. The T4 map (20) puts ipIII 3' to the lysozyme gene, and the amino terminal amino acid sequence of ipIII has been determined (21). There is only one discrepancy between the predicted first 11 amino acids and those determined from protein sequencing, a threonine versus a valine. We consider this proof that this site is the start of ipIII and have included it in Table 2. The one discrepency is probably due to either strain differences or a sequencing error.

CONCLUSION

There are two advantages to this method of defining a functional site over the more conventional consensus sequence approach. The first is that we have specified nothing about the functional sequences except their inclusion in that class. The algorithm finds a weighting of all the features (bases at particular positions) that serves to distinguish the classes. No single

¹From the previous paper (1), rule 2 finds all sequences of (AGG, GGA or GAG) followed by ATG after 6 to 9 unspecified bases.

²⁰nly the first 720 bases were searched since the sequences from the two references disagree after than point.

³⁰nly the sequence following the tRNA genes was searched.

feature is totally required; only the weighted sum of all the features is important. This is in complete agreement with the observation that only the central U of the initiation codon is absolutely conserved in all known in vivo translational start sites.

The second advantage is that each site is evaluated quantitatively. This is especially useful in using the method to predict sites, because one can order the sites found. For example, using W71 to evaluate the T4 e and IPIII sequence, both genes are found and two nongenes are found, but the genes are evaluated three to six times higher than the nongenes. W51 finds no sites on the lexA sequence, but the site which is given the highest value is the correct gene beginning. We would like to believe that the value given to each sequence reflects its "strength" as an initiation site, but that is probably not true. If we examine genes that we know are translated in large amounts, such as the ribosomal proteins and phage coat proteins, their values lie in the upper half of the gene distributions (as in Fig. 10), but are not clustered at the top end. If we knew the relative translational efficiencies of a large number of the genes, we could include that in the training process and require that values correlate with "strength". Unfortunately, very few quantitative comparisons have been made.

This paper is the second report we have made, using a different approach, that demonstrates information relevant to ribosome initiation besides the initiation codon and the Shine and Dalgarno sequence (1). Interactions between the ribosome and specific sequences (other than the Shine and Dalgarno) have not been demonstrated. We think that these other informational bases influence the rates at which some of the partial reactions involved in initiation occur (22).

Finally, we note that the perceptron as constructed here scans linear sequences. We have reason to be wary of entirely linear investigations of information in an RNA molecule, although the data we obtained are interesting. We would be less wary of linear investigations of information within sequences that represent sites used on double-helical DNA.

Accordingly, we will next use the perceptron on promoters, a complex class of sequences recognized during transcriptional initiation.

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